

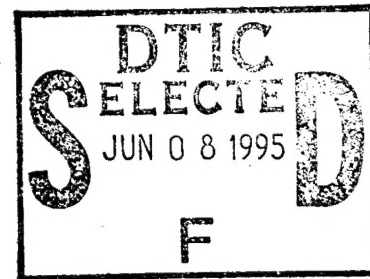
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**LASER-INDUCED ACOUSTIC AND SHOCK WAVES IN  
OCULAR TISSUES**

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# GENERATION AND PROPAGATION OF ACOUSTIC AND SHOCK WAVES IN OCULAR TISSUES (THEORY)

## INTRODUCTION

Analytical equations that describe generation and propagation of acoustic and shock waves in biological tissues are presented. Several practical situations of laser irradiation of various ocular tissues are considered: thermoelastic generation of acoustic waves, linear and nonlinear effects that occur upon propagation of stress transients in tissues, cylindrical shock wave generation upon plasma optical breakdown in the caustic of a focused laser beam, and spherical shock wave generation upon thermal explosion of melanosome.

Laser irradiation of ocular tissues can lead to the following two major types of physical processes: heat generation and an optical breakdown. It is tissue absorption coefficient and laser intensity that determine the type of laser-tissue interaction mechanisms. In cases where tissue is strongly absorbing and laser radiation is not strongly focused in a medium, fast nonradiative relaxation of the excited states converts absorbed laser energy into heat. Also, when tissue is transparent for the laser light, the only process that allows laser energy to be deposited in tissue is plasma optical breakdown by the high electric field in a focused laser beam. Optical breakdown can also occur when strongly absorbing tissue is superheated to a temperature of several thousand degrees.

Generation of acoustic waves by the consecutive transformation of light energy into heat and then to mechanical stress is the most essential phenomenon upon short-pulse laser irradiation of absorbing tissues. Thermo-optical generation of acoustic waves of high amplitude and formation of shock waves because of nonlinear propagation in various materials have been investigated and reviewed in the literature.<sup>1-10</sup> Short laser pulses allow the most efficient realization of thermoelastic stress induction because of minimal stress relaxation during laser heating (see also section on Stress Relaxation). There are a number of publications devoted to various mechanisms of generation and propagation of short-pulse, laser-induced shock waves in water containing tissues.<sup>11-14</sup> Plasma optical breakdown in water and water containing tissues has been experimentally investigated (see, for example, publications by Vogel<sup>11</sup> and Docchio.<sup>15</sup>) However, theoretical considerations of optical breakdown are not as thorough as experimental studies.

Existing literature is lacking analytical equations which may allow simple estimations of acoustic-mechanical effects of laser pulses on ocular tissues. Unfortunately, analytic solutions of thermodynamic equations can not be obtained in many general cases that describe laser induced acoustic and shock waves.

## GENERATION AND PROPAGATION OF ACOUSTIC AND SHOCK WAVES

### Laser-induced Thermoelastic Stress

Let us consider an interaction of a laser pulse with soft biological tissue with properties close to that of water. Let irradiance incident to the tissue surface be:

$$I(x, y, t) = I(x, y)L(t) \quad (1)$$

where  $L(t)$  is the normalized time-function that defines the temporal profile of the laser pulse ( $0 < L(t) < 1$ ). The characteristic duration of laser pulse is  $\tau_L$ . The spatial distribution of a laser beam usually has a Gaussian profile in the x-y plane

$$I(x, y) = I_0 \exp[-(x^2 + y^2)/a^2] \quad (2)$$

where  $a$  is the characteristic radius of the laser beam. Let the laser radiation propagate along the z-axis. Because a laser beam radius is substantially smaller compared to the dimensions of irradiated tissue, we may assume that tissue is infinite in dimensions and occupies the half space  $z > 0$ .

The pressure distribution (a Laplasian pressure) in tissue can be described by the wave equation:

$$\Delta P - \frac{1}{C_s^2} \frac{\partial^2 P}{\partial t^2} = \frac{\beta}{C_p} \frac{\partial Q}{\partial t} \quad (3)$$

where  $P$  is the pressure,  $C_s$  is the speed of sound,  $t$  is time,  $\beta$  is the volume coefficient of thermal expansion,  $C_p$  is the heat capacity at constant pressure,  $Q$  is the spatial and temporal profile of heat distribution.

$$Q(x, y, z, t) = T\mu_a I(x, y) \exp(-\mu_{\text{eff}} z) L(t) \quad (4)$$

where  $T$  is the optical transmittance through the tissue boundary dependent on the specular reflection coefficient and the shape of tissue surface,  $\mu_a$  is the tissue absorption coefficient, and  $\mu_{\text{eff}}$  is the effective attenuation coefficient.

### Stress Transients in the Far Zone

An analytic solution of Equation (3) can be found outside the optical zone in the region located at the distance  $R \gg a$ ,  $\mu_a^{-1}$ . Acoustic pressure in this case can be expressed in a very general case of laser irradiation as:<sup>3</sup>

$$P = -\frac{T\beta a^2 I_0}{4\pi C_p R \tau_\mu^2} \int_0^\infty \exp\left(-\frac{k^2 S^2}{4}\right) \frac{k^2}{1+k^2} \exp(ik\gamma) F\left(\frac{k}{\tau_\mu}\right) dk \quad (5)$$

where we introduced the following symbols:  $k = \omega \tau_\mu$ ,  $\gamma = (R/C_s - t) \tau_\mu^{-1}$ ,  $S = \tau_a/\tau_\mu$ ,  $R$  is the distance from center of our coordinate system to the observation point,  $\tau_\mu = \cos\theta/\mu_a C_s$ , and  $\tau_a = a \sin\theta/C_s$  are characteristic delay times for the ultrasound waves propagating from elementary sources in the  $z$ -direction and in the  $x$ - $y$  (surface) plane respectively,  $\theta$  is the angle between the  $z$ -axis and the direction to the point of observation,  $F(\omega)$  is the acoustic spectrum of laser-induced stress transients after the end of laser pulse, and  $\omega$  is the modulation frequency of laser intensity. Laser pulse spectrums can be expressed as follows:

$$F(\omega) = \int_0^\infty L(t) \exp(i\omega t) dt \quad (6)$$

Let us consider various limit cases when one can neglect the delay between moments of acoustic wave arrival time to the point of observation from elementary sources located along the  $z$ -axis of laser incidence ( $\tau_L$  relative to  $\tau_\mu$ ) and in the plane perpendicular to the laser beam ( $\tau_L$  relative to  $\tau_a$ ).

(1) In the case when  $\tau_L \gg \tau_a$  and  $\tau_L \gg \tau_\mu$  Equation (5) can be given as:

$$P(z) = -\frac{T\beta a^2 I_0}{4\pi C_p R \tau_\mu} \cdot \frac{\partial^2 L}{\partial \left(t - \frac{R}{C_s}\right)^2} \quad (7)$$

In this case the profile of laser-induced stress transient has characteristic M-shape (the second differential from a bell-shaped laser pulse), and its parameters do not depend on laser intensity distribution over the surface ( $x$ - $y$ ) plane.

(2) In the case when  $\tau_L \gg \tau_a$  and  $\tau_L \ll \tau_\mu$  the irradiated volume with heat sources has the shape of an elongated cylinder. The Equation (5) can be presented in this case for a **narrow laser beam** as:

$$P(z) = -\frac{T\beta a^2 I_0}{4\pi C_p R \tau_\mu} \left\{ L\left(t - \frac{R}{C_s}\right) - \pi \frac{F^*(\omega)}{\tau_\mu} \exp\left(-\left|t - \frac{R}{C_s}\right|\right) \right\} \quad (8)$$

where  $F^*(\omega)$  in this case is just an integral over the pulse temporal profile,

$$F^*(\omega) = \int_0^\infty L(t) dt.$$

For long laser pulses with duration  $\tau_L \gg \tau_a$  the transient stress temporal profile does not depend on the stress relaxation ratio  $S = \tau_a/\tau_\mu$  but is determined by the temporal profile of the laser pulse,  $L(t)$ .

$$(3) \quad \tau_\mu \ll \tau_L \ll \tau_a.$$

Let us now consider the case of short laser pulses, when heat generation time is shorter compared with stress propagation time along the tissue surface, but not along optical attenuation depth. In this case the equation for acoustic pressure can be given as:

$$P = -\frac{T\beta a^2 I_0}{16C_p R \tau_\mu^2} F^*(\omega) \cdot \left\{ \frac{4}{\sqrt{\pi} S} \exp\left(\frac{\gamma^2}{S^2}\right) - \exp\left(\frac{S^2}{4}\right) \cdot \left[ \exp(-\gamma) \operatorname{erf}\left(\frac{s}{2} + \frac{\gamma}{s}\right) + \exp(\gamma) \operatorname{erf}\left(\frac{s}{2} - \frac{\gamma}{s}\right) \right] \right\} \quad (9)$$

$$\text{where } \operatorname{erf}(z) = \frac{2}{\pi} \int_z^\infty \exp(-t^2) dt.$$

In the case of confined stress conditions of irradiation with a **wide laser beam**, the z-axial profile of laser-induced stress is independent on the temporal profile of the laser pulse and is defined by the stress relaxation ratio,  $S$ . Two limit cases can be considered.

(a) Laser irradiated volume (the region of heat sources) has a shape of a flat disk. In this case  $S \gg 1$  and Equation (9) can be modified as:

$$P = -\frac{T\beta a^2 I_0}{\sqrt{\pi} c_p R \tau_\mu^2 S^3} F^*(\omega) \cdot \left[ \frac{2 \left( t - \frac{R}{C_s} \right)^2}{\tau_a^2} - 1 \right] \exp \left[ -\frac{\left( t - \frac{R}{C_s} \right)^2}{\tau_a^2} \right] \quad (10)$$

(b) Laser irradiated volume (the region of heat sources) has a shape of an elongated cylinder. In this case  $S \ll 1$  and Equation (9) can be given as:

$$P = -\frac{T\beta a^2 I_0}{8c_p R \tau_\mu^2 S} F^*(\omega) \cdot \left\{ \frac{2}{\sqrt{\pi}} \exp \left[ -\frac{\left( t - \frac{R}{C_s} \right)^2}{\tau_a^2} \right] - S \exp \left[ -\frac{\left| t - \frac{R}{C_s} \right|}{\tau_\mu} \right] \right\} \quad (11)$$

Practical note: The above given equations are applicable in certain ranges of observation angles.

Equation Number	Observation Angle Range	Equation Number	Observation Angle Range
(7)	$30 \leq \theta \leq 70$	(10)	$60 \leq \theta \leq 90$
(8)	$0 \leq \theta \leq 45$	(11)	$30 \leq \theta \leq 60$

(4)  $\tau_L \ll \tau_a$  and also  $\tau_L \ll \tau_p$

In the case of flat disk geometry of irradiation ( $\mu_a \gg a$ ) with a short laser pulse when not only  $\tau_L \ll \tau_a$ , but also  $\tau_L \ll \tau_p$ , Equation (5) for the temporal distribution of the pressure wave can be solved analytically as:

$$P(t) = \left( \frac{E_o \beta C_s a^2 \tau_\mu}{2\pi R \tau_a^2} \right) \frac{\partial^2 F}{\partial y^2} \Big|_y \quad (12)$$

where  $E_o$  is the laser pulse energy, and  $y' = (C_s t - R)/\sin\theta$  is the distance on the y-axis chosen in the direction of projection of the observation point on the tissue boundary, and  $F(y) = \int I(x, y) dx$  is the function that characterizes the effective distribution of elementary heat sources along the y-axis.

### Stress Transients in the Near Zone

Characteristic features of acoustic transient pulses, induced by laser pulses in the near zone, can be obtained from the consideration of a simple one-dimensional model.

Let the energy  $E_{abs}$  be absorbed in a sphere with radius  $r_o$  (assume melanosome).

**Sphere.** When  $r_o \gg c_s \tau_L$  the maximal pressure value in the spherical acoustic wave is:

$$P = \frac{3}{16\pi} \cdot \frac{E_{abs} \beta C_s^2}{C_p r_o^2 R} \quad (13)$$

In this case, amplitude of pressure is determined by the absorbed energy, and the acoustic pulse duration is equal to  $r_o/c_s$ .

When  $r_o \ll c_s \tau_L$  the maximum pressure value equals:

$$P = \frac{3}{16\pi} \cdot \frac{E_{abs} \beta C_s}{C_p r_o R \tau_L} \quad (14)$$

In this case, pressure amplitude is determined by the rate of thermal energy deposition, and acoustic pulse duration is equal to the laser pulse duration. If the irradiated volume has an acoustic impedance mismatch with the medium around it, the temporal profiles of laser-induced acoustic waves have characteristic N-shape (compression pulse followed by the rarefaction pulse).

The efficacy of the thermo-optical mechanism of stress generation in absorbing sphere is described by the equation:

$$\eta_s \equiv \frac{1}{4} \left( \frac{\beta C_s}{C_p} \right)^2 \frac{Q}{\rho} \quad (15)$$

**Flat Disk.** Let the energy  $E_{abs}$  be absorbed in a flat disk with thickness equal to  $1/\mu_{eff}$  (assume relatively wide laser beam incident on the layer of pigmented epithelium). Thermal expansion of the instantaneously heated medium causes a pressure-rise,  $P_o$ , in the irradiated volume. This pressure is proportional to the thermal coefficient of volume expansion,  $\beta[K^{-1}]$ , of the given medium:

$$P_o = (1/\gamma) \Delta V / V = (1/\gamma) \beta \Delta T \quad (16)$$

where  $\gamma$  [ $\text{bar}^{-1}$ ] is thermodynamic coefficient of isothermal compressibility:

$$\gamma = (C_p / C_v) * (1 / \rho) \quad (17)$$

Substituting the Equation (17) for the temperature rise,  $\Delta T$

$$\Delta T = E_{abs}(z) / \rho C_v \quad (18)$$

one can get maximal pressure magnitude expressed as:

$$P_o = (\beta C_s^2 / C_p) \Phi_o \mu_a = \Gamma \Phi_o \mu_a \quad (19)$$

where  $C_s$  [cm/s] is the sound velocity in medium,  $\Delta V[\text{cm}^3]$  is the volume increase caused by the thermal expansion,  $V$  is the laser-irradiated volume initially at room temperature,  $\rho[\text{g}/\text{cm}^3]$  is the tissue density,  $C_p$  [J/gK] is the heat capacity at constant pressure,  $C_v$  is the heat capacity at constant volume,  $E_{abs}$  [J/cm<sup>3</sup>] is the absorbed energy density,  $\Phi_o$  [J/cm<sup>2</sup>] is the laser energy fluence incident at the absorbing medium, and  $\mu_a$  [cm<sup>-1</sup>] is the absorption coefficient of the ocular tissue.

The efficacy of the thermo-optical mechanism of stress generation for the flat disk geometry is described by the expression similar to that for a sphere except a numerical factor.

$$\eta_d = \frac{1}{2} \left( \frac{\beta C_s^2}{C_p} \right) \frac{Q}{\rho} \quad (20)$$

The expression  $(\beta C_s^2/C_p)$  in Equation (20) represents the Grüneisen parameter,  $\Gamma$ , which is proportional to the fraction of heat that generates mechanical stress. The value of the  $\Gamma$ -parameter of water and aqueous solutions equals 0.11 at 20° C and rises to 0.125 at 25° C and to 0.5 at 100° C.

Figure 1 shows Grüneisen coefficient as a function of temperature for water and some biological tissues. Linear dependence that is accurate for water is assumed to be valid for water-containing tissues.

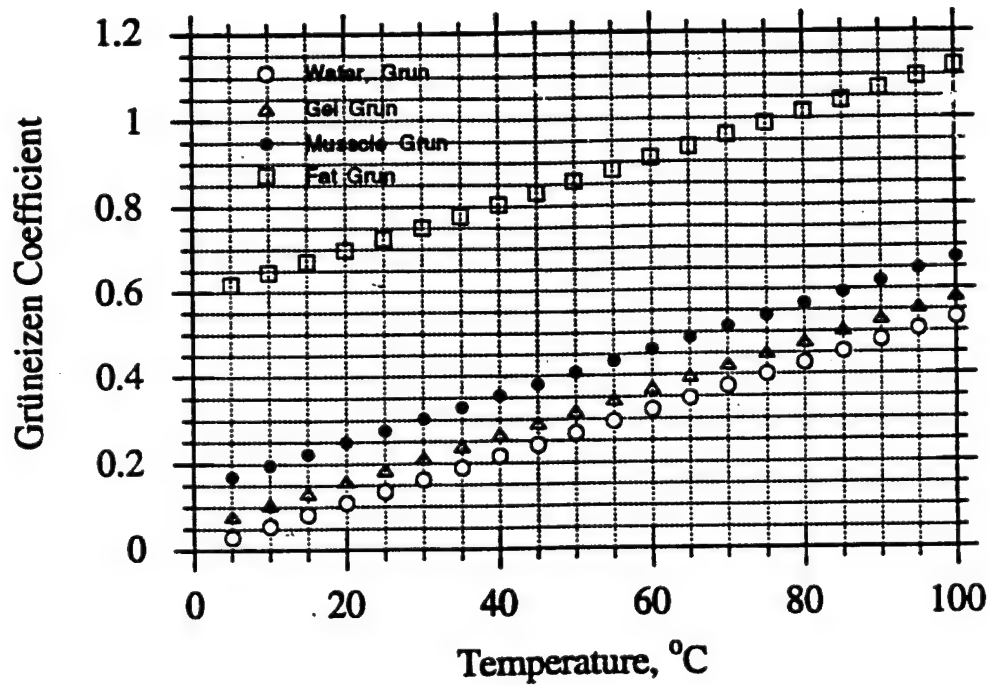


FIGURE 1. G factor for water and tissues as a function of temperature.

### **Shock Wave Generation upon Plasma Optical Breakdown on the Surface of Pigment Epithelium**

The interaction of an intense short laser pulse with the surface of pigmented epithelium is discussed below. Optical breakdown and formation of a plasma cavity can be observed upon high-intensity, short-pulse irradiation.<sup>11-15</sup> Expansion of the plasma cavity at the end of a laser pulse can give rise to an intense pressure pulse in ambient water of ocular tissue. In many cases, the plasma cavity has a cylindrical shape. Therefore, expansion of the plasma cavity leads to the formation and propagation of cylindrical shock waves in ocular tissues containing water. Subretinal and preretinal hemorrhages and mechanical disruption of intraocular tissues were observed and investigated as a result of optical breakdown reported from numerous studies.<sup>16-20</sup>

#### **Shock Waves from Cylindrical Plasma-Cavity**

Let us consider plasma-channel (plasma-cavity) formation with the shape of an elongated cylinder with initial radius  $R_i \sim 10^{-3}$  cm and length,  $L$ , as a result of pulsed laser heating. We assume that low temperature plasma with initial temperature of  $T_i \sim (5 - 15) \cdot 10^3$  K and pressure  $P_i \sim 10^2 - 10^5$  bar is generated in the optical breakdown.

Laser energy absorbed by the plasma will be spent for the increase of plasma internal energy and the work of plasma-cavity expansion:

$$\frac{dW}{dt} + P \frac{dV}{dt} = \frac{dE}{dt} \quad (21)$$

or

$$W(t) + A(t) = E(t) \quad (22)$$

where  $V = S L = \pi R^2 L$  is the volume of cylindrical plasma-cavity with radius  $R$ ,  $E = E_{\text{abs}}$  is the absorbed laser energy.

Because plasma is relatively low density, the internal plasma energy,  $W$ , can be approximated with the equation for the energy of the ideal gas:

$$W = \frac{PV}{\gamma - 1} \quad (23)$$

where  $\gamma$  is the adiabatic parameter of ideal gas.

For plasma formed from water at temperatures about  $10^4$  K, which correspond to the first ionization energy threshold for water, the value of adiabatic parameter  $\gamma$  equals 1.26.

The work,  $W_{\text{expansion}}$ , necessary for the plasma-cavity expansion is equal to:

$$W_{\text{expansion}} = \int_{R_i}^R P l ds \quad (24)$$

Internal homogeneous pressure in the plasma channel is determined by the solution of the system of equations, which describes the plasma channel expansion in ambient water (of ocular tissue) using the Kirkwood-Bethe model with initial and boundary conditions:

$$\frac{du}{dt} \left( 1 - \frac{u}{c'_s} \right) + \frac{3}{2} \frac{u^2}{R} \left( 1 - \frac{1}{3} \frac{u}{c'_s} \right) = \frac{1}{2} \frac{H}{R} \left( 1 + \frac{u}{c'_s} \right) + \left( 1 - \frac{u}{c'_s} \right) \frac{1}{c'_s} \frac{dH}{dt} \quad (25)$$

$$H = \frac{c_s^2}{n-1} \left[ \left( \frac{P+B}{A} \right)^{\frac{n-1}{n}} - 1 \right] = \int_{P_i}^P \frac{dP}{\rho} \quad (26)$$

$$P = A \left( \frac{\rho'}{\rho} \right)^n - B \quad (27)$$

where  $u = \frac{dR}{dt}$  is the rate of plasma-channel expansion,  $C_s$  and  $C'_s$  are respectively speed of sound in undisturbed water with density  $\rho$  and speed of sound in water (with density  $\rho'$ ) exposed to a stress,  $H$  is the enthalpy, and  $A$ ,  $B$ , and  $n$  are empirical constants (see also Equation (81) in the section titled Formation of a Shock Wave from High Amplitude Acoustic Waves).

The system (Equations 25, 26, 27) accounts for the influence of liquid compressibility when expansion channel velocity is substantial and is approximately equal to the speed of sound in water,  $C_s$ . This system of equations can be integrated numerically and shock wave amplitude in ambient water can be obtained if the equation for the energy deposition  $E(t)$  is known.

Some simple estimates of hydrodynamic parameters can be made without numerical integration of the system (Equations 25, 26, 27) formulated above. Let characteristic radius of cylindrical plasma channel be  $R_0$  at the end of laser pulse end with duration  $\tau_L$ . Then characteristic velocity of plasma expansion is given by  $u = R_0/\tau_L$  and characteristic pressure  $P_i$  in plasma channel can be expressed as:

$$P_1 = \rho u^2 = \rho \frac{R_o^2}{\tau_L^2} \quad (28)$$

Using Equation (28) and the energy balance Equation (21) one can obtain the following approximate equation for  $R_o$ :

$$R_o = \left[ \frac{(\gamma - 1)E_{abs}}{\pi \rho l} \right]^{1/4} \tau_L^{1/2} \quad (29)$$

and equation for  $P_1$  can be obtained from Equations (28 and 29):

$$P_1 = \frac{1}{\tau_L} \left( \frac{\rho(\gamma - 1)E_{abs}}{\pi l} \right)^{1/2} \quad (30)$$

where  $E_{abs}$  is the laser energy absorbed during time interval  $\tau_L$ , and  $l$  is the constant length of plasma-channel.

Pressure distribution in the acoustic wave propagating in a perpendicular direction to the axis of plasma-cavity is described by the following equation:<sup>19</sup>

$$P_1 = \frac{\rho R_o^4 l}{2\tau_L^2 d} \cdot \frac{L(t)}{\ln \frac{l}{R}} \quad (31)$$

where  $\tau = \frac{t}{\tau_p} - \frac{d}{c_s \tau_L}$  is the normalized time,  $d$  is the distance measured from the plasma-channel axis to the observation point,  $R$  is the radius of plasma-channel in the moment  $t$ ,  $R_o$  is the radius of plasma channel defined by Equation (29) and  $L(t)$  is the temporal profile of the laser pulse.

Maximum value of  $P_1$  equals:

$$P_1 = \frac{\rho R_o^2}{2\tau_L d} \quad (32)$$

assuming  $R_o^2 L(t) / \ln \frac{l}{R} \sim 1$ .

## Shock Waves from Spherical Plasma-Cavity

In some practical cases of focused laser irradiation or occurrence of self focusing effects, the characteristic diameter of the irradiation spot on the surface of the pigment epithelium (retina) is about 10  $\mu\text{m}$ . The characteristic thickness of pigment epithelium layer, the main absorber of laser pulse energy, is about 5-10  $\mu\text{m}$ . Therefore, in some short time after the end of the laser pulse, one may consider the shape of the plasma-cavity formed as a sphere. The expansion of the cavity produced by the thermally induced plasma leads to the formation and propagation of a spherical shock wave in ambient water of ocular tissue.

In this case laser-induced spherical plasma-cavity has initial radius  $R_i \sim 0.001$  cm, initial temperature  $T_i \sim (5-15) \cdot 10^3$  K, and pressure  $P_i \sim 10^2 - 10^5$  bar.

Equations (21, 22, 23) are also valid in this case, where  $V = 4/3\pi R^3$  and is the volume of plasma spherical-cavity with radius  $R$ .

Internal homogeneous pressure in the plasma-cavity is determined by the solution of the system of equations which describes the plasma expansion in water (tissue containing water) using the Kirkwood-Bethe model. This model accounts for the influence of liquid compressibility when the rate of plasma expansion is extremely high and approximately equals the speed of sound in water,  $C_s$ . The system has to be solved along with appropriate initial and boundary conditions.

$$\frac{du}{dt} \left( 1 - \frac{u}{c'_s} \right) + \frac{3}{4} \frac{u^2}{R} \left( 1 - \frac{1}{3} \frac{u}{c'_s} \right) = \left( 1 + \frac{u}{c'_s} \right) \frac{H}{R} + \left( 1 - \frac{u}{c'_s} \right) \frac{1}{c'_s} \frac{dH}{dt} \quad (33)$$

$$H = \frac{c_s^2}{n-1} \left[ \left( \frac{P+B}{A} \right)^{\frac{n-1}{n}} - 1 \right] \quad (34)$$

$$P = A \left( \frac{\rho'}{\rho} \right)^n - B \quad (35)$$

This system of equations describes the shock wave amplitude in ambient water and can be integrated numerically if the expression of energy deposition  $E(t)$  is given.

Simple estimations of hydrodynamic parameters can be made without numerical integration of the system (Equations 33, 34, 35). Let the characteristic radius of plasma-cavity be  $R_0$  at the end of the laser pulse,  $\tau_L$ . Then characteristic rate of plasma expansion is equal to  $u = R_0 / \tau_L$  and pressure  $P_1$  in the cavity can be written as:

$$P_1 = \rho u^2 = \rho \frac{R_o^2}{\tau_L^2} \quad (36)$$

Using Equation (28) and the energy balance Equation (21) one can obtain the following approximate equation for  $R_o$ :

$$R_o = \left[ \frac{3(\gamma - 1)}{4\pi\rho} E_{abs} \right]^{1/5} \tau_L^{2/5} \quad (37)$$

and equation for  $P_1$  can be obtained from Equation (36 and 37):

$$P_1 = \rho^{3/5} \left[ \frac{3(\gamma - 1)}{4\pi} \right]^{2/5} \frac{E_{abs}^{2/5}}{\tau_L^{6/5}} \quad (38)$$

For calculation of maximum amplitude of spherical shock wave the following equation can be employed:<sup>21</sup>

$$P = \frac{P_1 R_o}{2} g \exp\left(-\frac{t}{\theta}\right) \quad (39)$$

where parameter  $\theta = 1 + 2/g$ ,  $g = [M^{3/2} \sqrt{2 \ln\left(\frac{d}{R_o}\right)}]^{-1}$  is the factor accounting for the nonlinear extinction of the shock wave, and  $M = u/c_s = R_o / c_s \tau_L$  is the Mach number.

Equation (39) can be used in region placed far from the point of optical breakdown. In addition the following condition must be fulfilled:  $\ln \frac{d}{R_o} \geq \frac{1}{4M^3}$ .

On the basis of Equation (39) we can evaluate the shock wave energy and its relation to the laser energy absorbed by plasma, which characterizes the coefficient of laser energy transformation into the shock wave (acoustic) energy:

$$\eta = \frac{3}{2}(\gamma - 1) \left( M \cdot \ln \frac{d}{R_o} \right)^{1/2} \quad (40)$$

$\eta$  has maximum value of about 20-30 %.

Pressure amplitude,  $P_{\max}$ , on the front of a spherical shock wave can be estimated by interpolation of the following equation:

$$\frac{P_{\max}}{A} = \frac{8}{25} \frac{n}{n+1} \left\{ 0.611 \left[ \left( 1 + 0.16 \frac{nA}{E} R_*^3 \right)^{\frac{5}{18}} - 1 \right] \right\}^{-1} \quad (41)$$

where  $R_*$  [cm] is the radius of shock wave front,  $n = 7$ ,  $A = 3001$  bar,  $P_{\max}$  [bar] is the maximal pressure in the shock front, and  $E$  [J] is the absorbed laser energy.

The following condition must be satisfied (strong shock wave):  $P_{\max} > 0.02 P_0$  where  $P_0$  is the pressure value in water obtained using the equation of state for water from the system of Equations (33, 34, 35).<sup>22</sup>

This interpolation-equation (41) is transformed to the strong explosion solution near the breakdown point and precisely describes the extinction of shock wave at long distances of the observation point. Hydrodynamic and acoustical processes during laser breakdown of water and other liquids were experimentally investigated in numerous studies.<sup>23-27</sup>

### **Pressure Wave Generation upon Thermal Explosion of Melanosome**

#### **Evaporation of Water and Expansion of Vapor Bubble Initiated by Laser Heating of Melanosome**

Let a spherical melanosome of radius  $r_0 \approx 1 \mu\text{m}$  be situated in ocular tissue containing water and irradiated with a focused short laser pulse. Because of microscopic dimensions of the melanosome, heat exchange between adjacent water layers has to be considered simultaneously with the process of laser energy absorption by the melanosome. Water contained tissue has thermophysical parameters similar to that of water, and therefore, for simplicity we may consider a melanosome placed in water. Let the melanosome and the adjacent water layer be rapidly superheated to a temperature  $T^*$  higher than water evaporation temperature  $T_b = 100^\circ \text{C} = 373^\circ \text{K}$  as a result of a short laser pulse irradiation under the atmospheric pressure. In this case the water surrounding the melanosome can be transferred into the metastable state and undergo explosive vaporization. Phase transition (vapor generation) will occur only in the water layer that surrounds the melanosome. The thickness of this layer,  $\delta$ , can be calculated using the simple heat diffusion equation:<sup>28</sup>

$$\delta = \sqrt{4\chi\tau_L} - r_0 \quad (42)$$

It is experimentally established that the maximum value temperature  $T^*$  of intense homogeneous nucleation (explosive evaporation) can reach is  $T^* = 578\text{--}593 \text{ K}$  under short-pulse laser irradiation.<sup>29,30</sup> Practically, the process of explosive evaporation can be

initiated at the temperature value lying in the interval  $640 > T^* > 373$  K in various experimental situations. The higher the temperature of superheating, the shorter the time-delay between laser energy deposition and the moment of thermal explosion. The rate of vapor bubble formation,  $J(T)$ , expressed in  $[1/s \text{ cm}^3]$  is given by the Döring-Volmer equation modified by Stranski:

$$J(T) = n \left[ \frac{6\sigma}{\pi m \left( 2 + \frac{P'}{P''} \right)} \right]^{\frac{1}{2}} \exp \left( -\frac{W_c(T)}{kT} \right) \partial(\theta) \quad (43)$$

where  $n$  is the number of molecules per unit volume of superheated tissue,  $\sigma(T)$  is the surface tension of the superheated liquid medium at the temperature  $T^*$ ,  $m$  is the mass of the superheated liquid molecule,  $P'$  is the external pressure in tissue (or liquid),  $P''$  is the saturation vapor pressure in the bubble at  $T=T^*$ ,  $W_c(T)$  is the work of formation of the critical size vapor bubble,  $\partial(\theta) < 1$  is the coefficient of the angle of contact,  $\theta$ , that account for the decrease of  $W_c(T)$  because of the presence of the non-moistening surface of melanosome, and  $k$  is the Boltzman constant.

$$W_c(T) = \frac{16\pi\sigma^3}{3(P'' - P')^2} \quad (44)$$

The average delay time between the moment of laser energy deposition and the moment of critical size vapor bubble formation on the surface of superheated melanosome can be calculated as:

$$\tau_b = 1 / J V \quad (45)$$

We assume that the explosive evaporation of adjacent water layer occurs instantly, and the initial vapor layer around the melanosome also forms instantly at the moment,  $\tau_{10}$ , defined as:

$$\tau_{10} = \tau_0 + \Delta\tau_e \quad (46)$$

where  $\tau_0$  is the moment when the melanosome surface reaches the temperature,  $T^*$ , and  $\Delta\tau_e$  is the duration of explosion.

After instantaneous explosive vaporization, the spherical vapor bubble will be formed with initial radius  $r_{10} = r_0 + \delta$ , where  $\delta$  is the thickness of water layer superheated due to heat diffusion prior to explosion ( $\delta = 1-5 \text{ } \mu\text{m}$ ), and initial vapor temperature  $T_{10}$ , pressure  $P_{10}$  and density  $\rho_{10}$ . In this case, the pressure  $P_{10}$  and density  $\rho_{10}$  of the vapor equal correspondingly to the pressure,  $P_{1S}$  and density,  $\rho_{1S}$  of the saturated water vapor at

the temperature  $T_{10}$ . The mass  $M_{10}$  of the vapor bubble formed around the spherical melanosome and its initial outer radius  $r_{10}$  can be found from the system of three equations: mass conservation law (47), energy conservation law (48), and the equation of the saturated vapor state (49).<sup>31</sup>

$$V_{20}\rho_2 = M_{10} = V_{10}\rho_{1s}(T_{10}) \quad (47)$$

$$4\pi\rho_2 \int_{r_0}^{r_*} r^2 C_2 T(r) dr = (P_{10} - P_0)(V_{10} - V_{20}) + 4\pi r_{10}^2 \sigma + M_{10}(E_{10} + Q_v) \quad (48)$$

$$P_{10} = P_{1s} = R_g \rho_{1s}(T_{10}) T_{10} \quad (49)$$

where  $r^*=r$  at  $T=T^*$  is the radius of the volume in tissue where temperature,  $T$ , has reached the value of  $T^*$ , volume  $V_{10} = \frac{4}{3}\pi(r_{10}^3 - r_0^3)$  is the initial volume of vapor bubble produced from the water heated to the temperature  $T_{10}$  (vapor pressure equal that of saturation at  $T_{10}$ ), and  $V_{20} = \frac{4}{3}\pi(r_{20}^3 - r_0^3)$  is the total volume of water transformed into the vapor state (vapor bubble produced from the water layer with outer radius,  $r_{20}$ );  $C_1$ ,  $C_2$  [J/g °K] are respectively the heat capacity of vapor and water,  $R_g$  is the gas constant,  $\sigma$  [J/cm<sup>2</sup>] is the surface tension coefficient,  $Q_v$  is the specific heat (energy) of vaporization per unit mass,  $\rho_1$  and  $\rho_2$  are the densities of vapor and water respectively,  $P_1$  is the vapor pressure,  $P_0$  is the initial external pressure in water (tissue), distribution  $T(r)$  is determined from the solution of the heat conduction equation, which describes heat exchange between melanosome and adjacent water. Solution of the system of Equations (47, 48, 49) with the known value of  $T_{10}$  yields the initial parameters  $r_{10}$ ,  $\rho_{10}$ ,  $P_{10}$ ,  $M_{10}$  which can be used as initial conditions in consideration of the vapor bubble dynamics in aqueous ocular medium.

Let us assume a spherical vapor bubble expands according to the law  $R(t)$  with the rate  $dR/dt$  lower than the speed of sound in water,  $C_s$ . Let us also assume that water is absolutely incompressible. During adiabatic expansion the vapor pressure in the spherical bubble is described by the following equation:

$$P_1 = \rho_{10} \left( \frac{r_{10}}{R} \right)^{3\gamma} \quad (50)$$

where  $\gamma$  is the adiabatic exponent factor for water vapor. Raleigh equation, describing the bubble expansion process can be given as:

$$R \frac{d^2 R}{dt^2} + \frac{3}{2} \frac{dR^2}{dt} = \frac{1}{\rho} \left[ \rho_{10} \left( \frac{r_{10}}{R} \right)^{3\gamma} - P_0 \right] \quad (51)$$

Equation (51) can be integrated (solved) only using numerical methods with initial conditions. The pressure in compression wave originating by expanding bubble is described by the following equation:<sup>19</sup>

$$P = P_0 + \frac{R}{r} \left[ P_{10} \left( \frac{r_{10}}{R(t')} \right)^{3\gamma} - P_0 + \frac{1}{2} \rho_0 \left( \frac{dR(t')}{dt} \right)^2 \left( 1 - \frac{R^3(t')}{r^3} \right) \right] \quad (52)$$

where  $t' = t - r/C_s$ . If  $R(t)$  is known from Equation (52) one can obtain the pressure distribution that consists of the short compression pulse generated during initial stage of expansion under  $P > P_0$  followed by the longer pulse of rarefaction.

Accounting for compressibility of water, the pressure distribution in wave zone is determined by the linear acoustic solution:

$$P = P_0 + \rho_0 \frac{d^2 V(t')}{4\pi r} \quad (53)$$

where  $V = 4/3\pi R^3$ ,  $r$  is the radius to the point of observation,  $t' = t - r/C_s$ . Simple estimation of some parameters of compression wave gives the velocity of bubble expansion

$$\frac{dR}{dt} \sim \sqrt{\frac{P_{10}}{\rho_0}}, \text{ pressure in compression pulse } P \sim \frac{P_{10} r_{10}}{r}, \text{ duration of compression pulse, } \tau \sim r_{10} \sqrt{\frac{\rho_0}{P_{10}}}, \text{ energy of compression pulse } W \sim 4\pi r^2 \frac{P^2 \tau^2}{\rho_0 C_s}, \text{ a fraction of initial heat}$$

$$\text{energy of vapor, converted to energy of compression wave } Q_v \sim 3(\gamma - 1) \frac{r_{10}}{C_s \tau}.$$

Pressure distribution in an acoustic wave during initial stage of compression wave is described by the following equation:<sup>19</sup>

$$P = \rho_0 \frac{R_0^5}{\tau_L^2 r} \frac{f(t')}{R^2} \quad (54)$$

where  $R_0$  is determined by Equation (37),  $t' = \frac{1}{\tau_L} (t - \frac{r}{C_s})$ ,  $L(t')$  is determined by the temporal profile of the laser pulse, see Equation (1). Stress generation upon interaction of a short laser pulse with spherical particles placed in liquid and vapor bubble growth on particles was experimentally investigated by Golubnichiy et al.<sup>32</sup>

In the case when temperature  $T^*$  of explosive evaporation is only slightly higher compared with the threshold temperature of thermal explosion,  $dR/dt < C_s$ , equations presented above can be used to describe the linear acoustic wave generation. For

example, heating a melanosome to  $T_{10} = 120^{\circ} \text{ C}$  (393 K) causes a pressure-rise of about 2.2 bar. An acoustic wave with an amplitude of about 2-3 bar can not cause any significant damage to adjacent ocular tissues.

### **Thickness of Compressed Tissue in the Shock Front**

To determine the thickness  $d$  of the compressed tissue or water layer near the shock front, let us calculate the work ( $dW$ ) done in compressing a volume element  $dV$ :

$$dW = PdV \quad (55)$$

Substituting the coefficient of isothermal compressibility of tissue,  $\gamma$ , defined according to Equations (15 and 16) as:

$$\gamma = \frac{1}{V} \frac{dV}{dP} \quad (56)$$

in Equation (55) and integrating, one can obtain:

$$W = \frac{1}{2} V \gamma P^2 \quad (57)$$

For a spherical wave of radius  $R$ ,

$$W = 2\pi R^2 \delta \gamma P^2 \quad (58)$$

therefore,

$$\delta = \frac{W}{2\pi R^2 \gamma P^2} \quad (59)$$

## **STRESS WAVE PROPAGATION**

### **Stress Relaxation**

Consideration given in Stress Transients in the Near Zone is strictly valid only in the case when the process of heating is much faster than the process of medium expansion. It is said that "stress is confined" under such irradiation conditions. If stress is confined in a medium, the initial magnitude of the pressure in the heated volume may be expressed with Equation (19). In other words, the Equation (19) describes the initial, instantly generated

pressure amplitude prior to the stress wave propagation through the optical zone. It means that in this case the laser pulse duration,  $\tau_L$ , has to be much shorter as compared with the time it takes for the stress wave to propagate the distance equal to the effective penetration depth of light,  $l_{eff}$ . This condition of laser irradiation is referred to as "confined stress" condition.

$$\tau_{sr} = l_{eff} / C_s \gg \tau_L \quad (60)$$

The stress relaxation time,  $\tau_{sr}$ , is defined as the time it takes for the sound to propagate through the thickness of the irradiated volume. Taking into account that absorption in melanin granules dominates, we may neglect scattering in the retinal pigmented epithelium (RPE) and the process of heat diffusion can also, in principle, cause some decrease of the thermoelastic stress amplitude. However, the heat diffusion time,  $\tau_{hd}$ , in the vast majority of media (and particularly in ocular tissues) is much longer than the stress relaxation time,  $\tau_{sr}$ . Therefore, practically in all cases we can neglect the decrease of pressure in the irradiated tissue due to heat diffusion as compared with the stress relaxation.

When the stress relaxation parameter,  $\mu_a C_s \tau_L$ , is not very small, the measured pressure is lower than that calculated by the Equation (63). Stress relaxation changes both the amplitude and the shape of the pressure distribution generated in the sample. The actual acoustic pulse profile formed by the laser pulse profile,  $L(t)$ , can be calculated as the convolution of the instant spatial distribution of the thermoelastic sources moving into the media and temporal intensity envelope of deposited laser energy:

$$P(t) = \Gamma C_s \mu_a I_0 \int_{-\infty}^{+\infty} L(t) \exp(-\mu_a C_s |t - \tau_L|) dt \quad (61)$$

Temporal profiles of the Nd:YAG laser pulses used in our experiments can be described by the Gaussian distribution:

$$L(t) = (\pi)^{-1/2} \cdot \exp[(-2t / \tau_L)^2] \quad (62)$$

where  $\tau_L$  is the full pulse duration at 1/e of amplitude.

Equation (61) does not have a simple analytical solution and must be numerically calculated. In a more simple case of a rectangular temporal profile of a laser pulse, Equation (61) can be given by:

$$P(t) = \Gamma C_s \mu_a I_0 \frac{(1 - \exp(-\tau_L / \tau_{sr}))}{(\tau_L / \tau_{sr})} \quad (63)$$

When the laser pulse is long enough in comparison with  $1/(\mu_a C_s)$ , the profile of acoustic signal reproduces the derivative of the laser pulse shape.

$$P(t) = \Gamma \mu_a I_0 L(t) \tau_L \quad (64)$$

In the case of finite duration of laser pulses, the stress relaxation may affect only the amplitude of the generated acoustic signal if  $\tau_p$  is shorter than  $\tau_s$ . The amplitude of the acoustic signal drops down while its exponential wings change negligibly, because higher acoustic frequencies dissipate faster than low frequencies. Practically, the latter is valid when the confined-stress-parameter,  $\mu_{\text{eff}} C_s \tau_L < 1$ .

Figure 2 depicts the ratio of the real stress amplitude,  $P$ , that may be measured or calculated from Equation (63), and theoretically maximal amplitude,  $P_{\text{max}}$ , calculated from Equation (64) as a function of the stress relaxation parameter,  $\mu_{\text{eff}} C_s \tau_L$ .

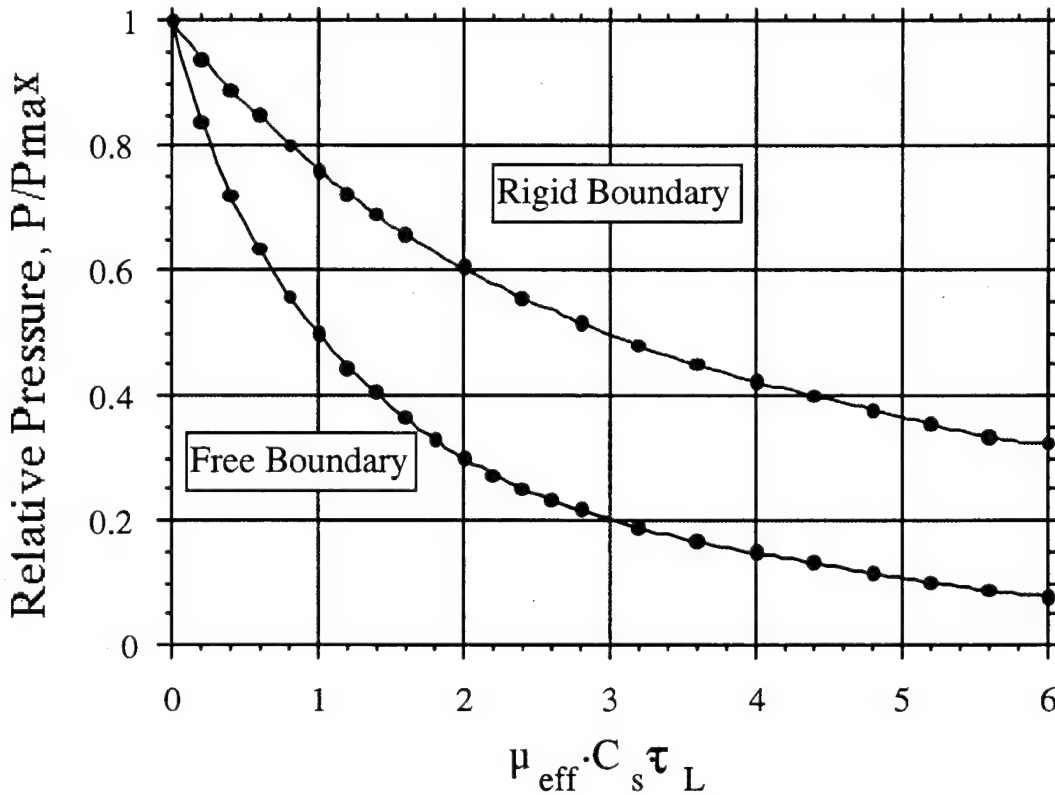


FIGURE 2. Theoretically calculated relative stress amplitude as a function of the stress relaxation parameter,  $\mu_a C_s \tau_L$ , in two cases of (a) "free" tissue boundary, (b) "rigid" tissue boundary.

There are two limit cases that can be considered for the boundary conditions between tissue and surrounding medium: (1) - "free" surface, when the acoustic impedance of tissue is much greater than the product of density,  $\rho$ , and the speed of sound for the medium (for example, air) above it, and (2) - "rigid" boundary, when the acoustic

impedance of tissue under heating is less as compared with that of any more dense medium (for example, detector plate) beneath it.

The stress relaxation in these two cases as a function of stress relaxation parameter has different behavior. In case of the "free" boundary, transient stress profile,  $S_f(t)$ , can be expressed as a derivative of the stress profile in the case of "rigid" boundary,  $S_r(t)$ .

$$S_f(t) = \frac{1}{\mu_a C_s} \cdot \frac{dS_r(t)}{dt} \quad (65)$$

Therefore, stress amplitude in the case of a free boundary decreases faster with the increase of laser pulse duration as compared with the case of "rigid" tissue boundary.

Wide laser beams incident on the eye can generate plane acoustic waves in the absorbing tissue of the RPE layer. However, focused laser beams of very small diameter may generate spherical or cylindrical acoustic waves. In cases where a stress wave is caused by the optical breakdown, the shape of an acoustic wave front will be presented by a plasma jet in the caustic of the focused laser beam. The stress wave propagation should be considered in the cylindrical geometry, where pressure magnitude decreases in proportion to  $1/\sqrt{r}$  with the increase of distance,  $r$ , from the source (see section titled Cylindrical Plasma-Cavity.). In cases where a laser beam is absorbed in a single melanosome that has a nearly spherical shape with diameter of about 1.5  $\mu\text{m}$ , generated acoustic waves will be represented by an expanding sphere, where pressure magnitude decreases as  $1/r$ , where  $r$  is the sphere radius (see section titled Spherical Plasma-Cavity).

### Acoustic Wave Reflection

At the onset of heat generation in the irradiated volume, a pressure wave propagates along the laser beam axis in the sample in two directions (one opposite to the other: into the sample and toward the sample surface). The value of the pressure amplitude propagating at the speed of sound,  $C_s$ , in each direction is equal to half of the initial amplitude of thermoelastic stress. Acoustic waves propagating toward the tissue surface may be reflected. The value of reflectance,  $R_{ac}$ , and its sign are defined by the mismatch of acoustic impedance,  $\rho C_s$ , at the boundary of tissue and surrounding medium.

The coefficient of acoustic wave reflection,  $R_{ac}$ , is equal to the ratio of pressure amplitudes of the incident,  $P_o$ , and reflected,  $P_{ref}$ , waves and can be calculated using the ratio of acoustic impedances as:

$$R_{ac} = \frac{P_{ref}}{P_o} = \frac{(1 - \rho C_s / \rho' C'_s)}{(1 + \rho C_s / \rho' C'_s)} \quad (66)$$

The Equation (66) indicates that in the case of "free" tissue boundary ( $\rho C_s \gg \rho' C'_s$ ), the reflected stress wave changes its sign and becomes a negative (tensile) wave. Therefore, the acoustic wave propagating into the tissue from the irradiated surface manifests itself as a "butterfly" with symmetric exponential wings formed by the axial light distribution (see Figure 3). In the case of the "rigid" tissue boundary ( $\rho C_s \ll \rho' C'_s$ ) acoustic reflectance,  $R_{ac}$ , has a positive sign, and the transmitted acoustic wave propagates into the more dense medium without sign change.

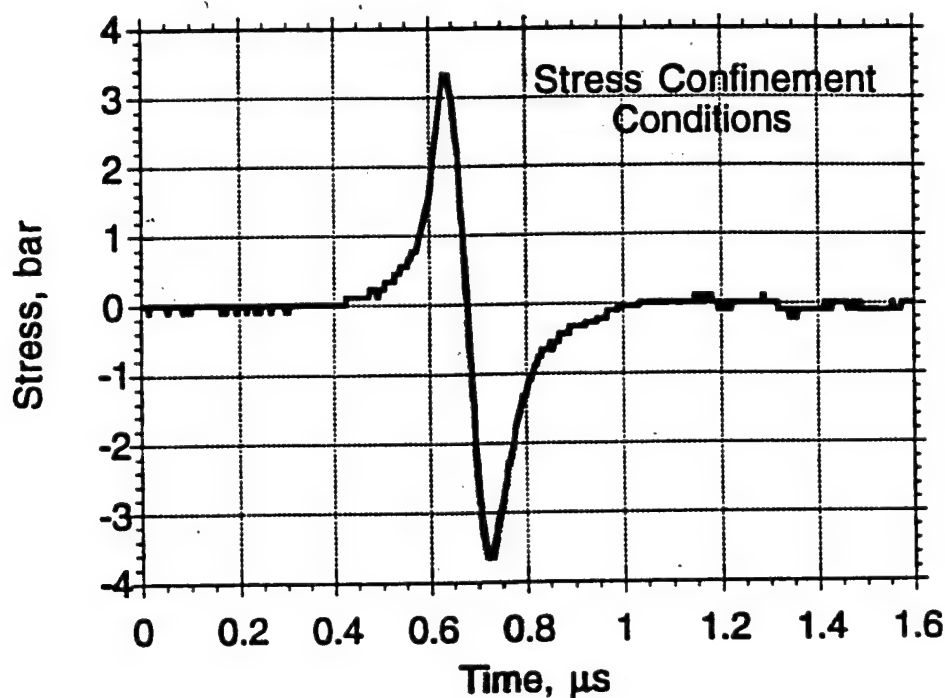


FIGURE 3. Laser induced transient stress in cornea irradiated at 266 nm in air under confined stress conditions.

### Acoustic Wave Transmission

As long as the sample under study is separated from the piezoelectric transducer by an acoustic conductor slab, it is essential to understand the process of stress transmission through a boundary between two media. Let us calculate the transmitted pressure amplitude in the case when the laser-induced plane acoustic wave propagates perpendicularly to the surface of an interface.

The transmitted intensity of the acoustic wave can be expressed as:

$$\frac{I_t}{I_i} = \frac{4\rho_i C_{s_i} \rho_t C_{s_t}}{(\rho_i C_{s_i} + \rho_t C_{s_t})^2} \quad (67)$$

where ultrasound velocities  $C_{s_i}$  and  $C_{s_t}$  and densities  $\rho_i$  and  $\rho_t$  are associated with the incident and transmitted waves, respectively. The acoustic wave intensity is proportional to the pressure amplitude squared:

$$I = P^2 / \rho C_s \quad (68)$$

Therefore, transmitted pressure may be given by:

$$T = \frac{P_t}{P_i} = \sqrt{\frac{I_t \rho_i C_{s_i}}{I_i \rho_t C_{s_t}}} = \frac{2\rho_i C_{s_i}}{(\rho_i C_{s_i} + \rho_t C_{s_t})} \quad (69)$$

There is an important and maybe at first unexpected conclusion, based on Equation (69): the pressure in the transmitted acoustic wave,  $P_t$ , can be higher than that incident upon the boundary. The value of the pressure transmittance,  $T$ , equals **2** when the acoustic impedance of the i-medium is much lower as compared to the acoustic impedance of the t-medium. In contrast, when stress propagates from melanosome into an aqueous environment, the transmitted pressure will be 1.13 times lower than that generated in melanin granule.

**Note:**

$$(\rho_{\text{water}} C_{s_{\text{water}}} = 1.0[\text{g/cc}] \cdot 1.49 \times 10^5 [\text{cm/s}]),$$

$$(\rho_{\text{tissue}} C_{s_{\text{tissue}}} = 1.1[\text{g/cc}] \cdot 1.77 \times 10^5 [\text{cm/s}]).$$

### **Alteration of an Acoustic Wave upon Propagation**

Spatial and temporal profiles of a laser-induced stress transient can be changed during propagation in ocular tissue. The measured signal can be altered by the medium due to the diffraction of the acoustic wave,  $D$ , as well as its attenuation,  $\Lambda$ , stress relaxation,  $R$ , and transmittance through interfaces,  $T$ , and by the tissue nonlinear acoustic properties. Acoustic nonlinearity can dramatically change the profile of a high-amplitude stress wave during its propagation in tissue causing formation of a shock front with dramatic pressure gradient (see section titled Formation of a Shock Wave from High-Amplitude Acoustic Waves).

Thus, the profile of an acoustic signal is determined by optical and acoustical properties of a medium as well as by the laser irradiation parameters, such as pulse duration, beam diameter, and energy fluence. The measured acoustic signal can be

generally described by the following equation that includes phenomena to be considered in the following sections.

$$P(z) = (\Gamma/2) \cdot \mu_a \cdot \Phi_0 \cdot R(z) \cdot T \cdot D(z) \cdot \Lambda(z) \cdot N \quad (70)$$

### Acoustic Wave Diffraction

The acoustic diffraction plays the most important role in the dissipation of thermoelastic waves. The reason for diffraction is the finite size of the area of stress-generation, which causes a gradual transformation of a plane wave into a spherical wave. The initial consequence of diffraction is the increase of effective area of the acoustic wave, which leads to a decrease of the pressure amplitude and change of the acoustic signal profile.

The effective diameter of the acoustic wave,  $w_{aw}$ , at a depth,  $z$ , within medium is expressed as:

$$w_{aw} = w_L \sqrt{1 + \left(\frac{z}{z_D}\right)^2} \quad (71)$$

where  $w_L$  is the laser beam diameter at the tissue surface, and  $z_D$  is the effective depth of diffraction.

$z_D$  is defined as:

$$z_D = \pi n w_{aw} = \frac{\pi f_s w_L^2}{C_s} \quad (72)$$

where  $f_s$  - acoustic wave frequency,  $w_L$  - laser beam diameter,  $C_s$  - velocity of acoustic wave propagation,  $n = w_L / \lambda$  is number of acoustic wavelengths, and  $\lambda = C_s / f_s$  which fits into the diameter of acoustic wave at the surface of the irradiated sample.

The acoustic wave frequency is defined by the optical properties of irradiated medium and the speed of sound in this medium:

$$f_s = \mu_{eff} \cdot C_s \quad (73)$$

Thus, the diffraction depth can be estimated as:

$$z_D = \pi \cdot \mu_{eff} \cdot w_L^2 \quad (74)$$

Substituting Equation (74) in Equation (71) we get the equation for the effective area of a plane acoustic wave as a function of sample thickness, optical attenuation coefficient and laser beam diameter:

$$w_{aw} = w_L \sqrt{1 + (Z / \pi \mu_{eff} w_L^2)^2} \quad (75)$$

Figure 4 shows effective acoustic beam diameter with respect to initial laser beam width for two acoustic frequencies, 0.55 MHz and 75 MHz. The diffraction process is efficient for low acoustic frequencies and small beam diameters. The integration of all thermoelastic sources of spherical acoustic waves to form the plane wave propagating toward the acoustic transducer occurs at the distance,  $Z$ , that is not less than  $5/\mu_{eff}$ . Therefore, an accurate measurement of low light attenuation requires absolutely larger thicknesses of the sample as compared to the case for high attenuation coefficient,  $\mu_{eff}$ . Figure 4 demonstrated that in case of low absorbing medium, the ratio of  $Z/Z_D$  can be substantial and diffraction has to be taken into account. In contrast, high acoustic frequencies are not affected by diffraction even when initial diameter is as low as 1 mm.

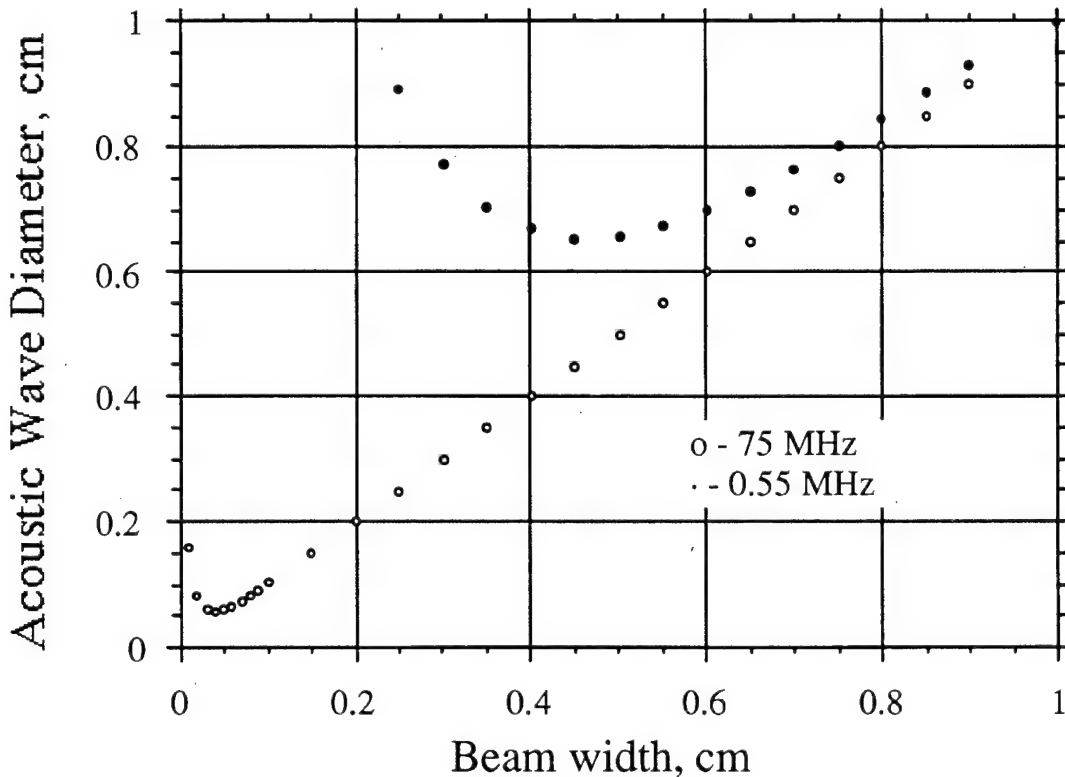


FIGURE 4. Demonstration of acoustic wave diffraction effect. The effective diameter of acoustic wave is plotted as a function of laser beam diameter according to Equation (77) for low (0.55 MHz) and high (75 MHz) acoustic frequencies.

The acoustic wave diffraction can be taken into account as the D-factor proportional to the ratio of laser beam area,  $A_L$  (or effective acoustic wave area at the sample surface), and acoustic wave area,  $A_{aw}$ , in the plane of interest on the z-axis given by:

$$A_{aw} = \pi w_{aw}^2 / 4 = (\pi / 4)(1 + (z / z_D)^2) w_L^2 \quad (76)$$

and ratio of acoustic wave areas at the sample and transducer surfaces is expressed by:

$$D = \frac{A_L}{A_{aw}} = \frac{1}{\left(1 + (z / z_D)^2\right)} = \frac{1}{\left(1 + \left(z \frac{z}{\pi \mu_{eff} w_L^2}\right)\right)} \quad (77)$$

Figure 5 depicts the diffraction parameter for highly absorbing and low absorbing solutions (i.e., high and low acoustic frequencies). Theoretical curves of the diffraction parameter, D, calculated according to the Equation (77) agree well with the experimental measurements of relative pressure magnitude as a function of laser beam diameter.

### **Acoustic Wave Attenuation**

The absorption and scattering of the acoustic wave energy causes an alteration of both the amplitude and exponential profile of the initial z-axial distribution of initial laser-induced stress. As far as we are interested in optical properties of media, it is convenient to combine acoustic absorption and scattering in one attenuation coefficient,  $\alpha$ , equal to the sum of acoustic absorption and scattering coefficients.

$$P(z) = P_0(z) \cdot \Lambda(z) = P_0(z) \exp(-\alpha(d-z)) \quad (78)$$

where  $P_0(z)$  is initial z-axial pressure distribution.

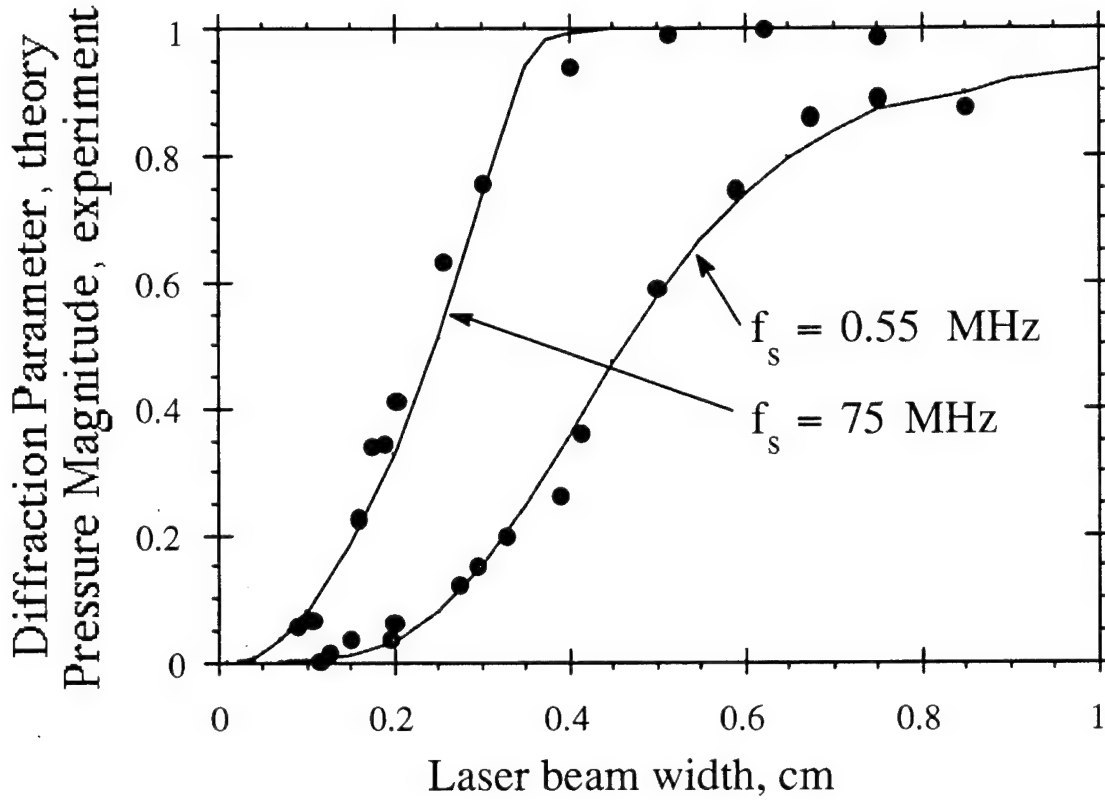


FIGURE 5. Diffraction parameter shown as a function of laser beam diameter in the case of low and high frequencies of acoustic wave. Experimental points are superimposed with theoretical curves, calculated based on Equations (77 and 78).

Equation (78) takes into account that during propagation toward the detector, subsurface stress will be attenuated stronger as compared to the stress generated in depth of tissue sample. Ultrasonic attenuation and other acoustic properties of biological tissues have been extensively studied after the invention of ultrasonic imaging.<sup>14</sup> Acoustic attenuation rises linearly with ultrasonic frequency for the vast majority of tissues. Acoustic attenuation coefficient in soft tissues is negligibly low in the frequency range of several hundred kHz that corresponds to optical attenuation,  $\mu_{\text{eff}}$ , about  $1\text{--}3\text{ cm}^{-1}$ . When acoustic frequency reaches 1 MHz, the value of  $\alpha$  increases to  $(0.01\text{--}0.05)\text{ cm}^{-1}$ . For high ultrasonic frequencies, above 10 MHz attenuation of acoustic waves becomes pronounced,  $(0.1\text{--}1.0)\text{ cm}^{-1}$ . In contrast to biological tissues, attenuation coefficient for acoustic waves in liquids has stronger frequency dispersion and proportional to  $f_s^2$  in the range (1-100) MHz. The attenuation of acoustic waves in pure water can be calculated as  $\alpha [\text{cm}^{-1}] = 2.5 \times 10^{-16} \cdot f_s^2 [\text{Hz}^2]$ .

#### **Formation of a Shock Wave from High-Amplitude Acoustic Waves**

The profile of high amplitude acoustic waves can be altered upon propagation in biological tissues. The major consequence of nonlinear propagation of high amplitude

acoustic waves in media is formation of shock waves (so called "relatively weak shock waves"). Shock front can be formed after the propagation at the distance  $L$ , that is dependent on the pressure amplitude,  $P_o$ , and the parameter of acoustic nonlinearity,  $\epsilon$ , of the given tissue ( $\epsilon=3.5 - 6.0$  for soft tissues).

$$\epsilon = 1 + \frac{\rho}{2C_s^2} \frac{\partial C_s^2}{\partial \rho} \quad (79)$$

The distance of shock wave formation can be expressed the following ways:

$$L_{sh} = \frac{\lambda_{ac}}{2\pi\epsilon M} = \frac{l\rho C_s^2}{\epsilon P_o} = \frac{\rho C_s^3}{2\pi\epsilon P_o f_{ac}} \quad (80)$$

where  $M = v_p / C_s$  is the Mach number, the ratio of particles velocity in the acoustic wave and the speed of sound in tissue,  $l$  is the length of the acoustic pulse in the direction of the laser beam, maximal pressure amplitude can be estimated using Equation (18).

**Practical examples** to be used for simple estimations of laser interactions with ocular tissue.

(1) Nanosecond laser pulse at 2.1- $\mu$ m wavelength produces acoustic transients in a RPE layer with amplitude of  $P_o=1$  bar and frequency of 100 MHz. Taking  $\rho=1.1$  g/cm<sup>3</sup>,  $C_s = 1.6 \cdot 10^5$  cm/s,  $\epsilon=5.0$  one can get the distance of the shock wave formation  $L=0.11$  mm.

(2) It was experimentally observed that a stress transient with acoustic pressure amplitude of approximately 20 kbar and pulse duration of about 0.75 ns can be generated upon irradiation of water by a short laser pulse with  $\tau_L = 80$  ps, 2.94-nm wavelength, laser pulse energy of 60 mJ, and intensity of 10 GW/cm<sup>2</sup>.<sup>6</sup> Estimation of  $P_o$  using the Equation (18) and value for  $\Gamma=0.3$  gives the value  $P_o = 30$  kbar in accordance with experimental value  $P_o = 20$  kbar. The empirical "equation of state" for water is:

$$P = A \left( \frac{\rho'}{\rho} \right)^n - B \quad (81)$$

where  $A=3.001$  kbar,  $B=3.0$  kbar,  $n=7$ , and  $\rho'=1.3\rho$  is water density at 20 kbar pressure.<sup>15</sup> From the simple system of equations for shock wave

$$P = \rho v_p C_{sh} \quad (82)$$

$$\rho' = r (C_{sh}/C_{sh}-v_p) \quad (83)$$

one can calculate that the shock wave velocity  $C_{sh} = 2.9 \cdot 10^5$  cm/s is about twice higher compared with the speed of sound in water, and the velocity of particles in liquid,  $v_p = 6.9 \cdot 10^4$  cm/s is about twice lower compared with the speed of sound,  $C_s$ .

Intensity of sound energy is equal to:

$$I_s = \rho C_{sh} v_p^2 = 1.85 \cdot 10^8 \text{ W / cm}^2 \quad (84)$$

and efficacy of conversion of optical energy into the mechanical stress energy is

$$\eta = \frac{I_s \tau_s}{I_o \tau_L} = 5.8\% \quad (85)$$

(3) Let us discuss the case of free surface of liquid irradiated with a short laser pulse. The following one-dimensional equation can be drawn for the plane (flat disk) geometry of irradiation:<sup>7</sup>

$$P = \frac{\beta I_o}{\mu_a C_s t_{\max}} \cdot 3(\Theta'^2 - \Theta'^3) \exp 3(1 - \Theta'), \text{ for } \Theta' \geq 0 \quad (86)$$

where  $t_m$  is the rise time of the laser pulse at maximum value of intensity,  $\Theta' = \frac{t - z / C_s}{t_m}$ ,

$a \gg 1 / \mu_{\text{eff}}$

Temporal profile,  $L$ , of the laser pulse can be approximated by a simple equation:

$$L(\Theta) = \Theta^3 \exp[3(1 - \Theta)] \text{ for } \Theta \geq 0 \quad (87)$$

The Equation (86) represents a bipolar pressure pulse with a positive *extremum* at  $\Theta = 0.42$  with the stress peak amplitude:

$$P_{\max}(\Theta' = 0.42) \approx 0.09 \frac{\beta I_o}{\mu_a C_p t_{\max}} e^3 \quad (88)$$

followed by a smaller negative *extremum* at  $\Theta' = 1.58$  with an amplitude:

$$P_{\max} (\Theta' = 1.58) \approx -0.04 \frac{\beta I_0}{\mu_a C_p t_m} e^3 \quad (89)$$

Therefore  $P_{\max}$  is inversely proportional to  $\mu_a$  for extremely strongly absorbing media. These equations are in good agreement with experimental data. For example, in Cleary and Hamrick<sup>9</sup> and Cleary<sup>10</sup> laser-induced stress transients in the mammalian eye resulted from the absorption of Q-switched ruby laser pulses with duration of about 100 ns and spot diameter of 750  $\mu\text{m}$ . Stress amplitudes were measured at the level of 100-1000 bar in the immediate vicinity of the site of absorption on the rabbit retina. The minimum pressure amplitudes encountered in the energy - density region associated with minimal threshold lesions are of the order of 10-30 bar.

The general system of equations that describes a profile of a pressure wave generated upon impact or expansion of a medium with velocity,  $v_m$  is given below.

Continuity equation:

$$\frac{\partial \rho}{\partial t} + \frac{\partial}{\partial z}(\rho v_m) = 0 \quad (90)$$

Conservation of impulse:

$$\frac{\partial}{\partial t}(\rho v_m) + \frac{\partial}{\partial z} \left( P + \rho v_m^2 - \frac{4}{3} \eta \frac{\partial v_m}{\partial z} \right) = 0 \quad (91)$$

Conservation of energy:

$$\frac{\partial}{\partial t} \left( \rho \epsilon + \frac{\rho v_m^2}{2} \right) + \frac{\partial}{\partial z} \left[ \rho v_m \left( \epsilon + \frac{v_m^2}{2} \right) + \rho v_m - \frac{4}{3} \eta v_m \frac{\partial v_m}{\partial z} - \kappa \frac{\partial T}{\partial z} \right] = 0 \quad (92)$$

where  $\epsilon = 4.2 \text{ kJ/g K}$  is specific heat of water evaporation,  $\kappa = 0.56 \text{ W/m g}$  is the thermal conductivity of water, and  $\eta$  is the coefficient of dynamic viscosity.

When speed of ultrasonic wave as a function of pressure amplitude is known, one can compute the system (Equations 94, 95, 96) to find out whether initial stress transient will be converted into a shock upon propagation or dissipation will dominate.

### Heating of Tissue by a Shock Wave

Although the laser radiation does not penetrate into the "cold" zone (heat diffusion is absent for the nanosecond pulses), the shock wave does propagate far beyond the point of generation. One of the side effects of the shock wave to adjacent tissue layers can be the heating of tissue due to the adiabatic compression by a shock wave<sup>33</sup> where  $u_s$  is the mass velocity (particles velocity) in the shock wave.

$$\Delta T = \frac{C_s T \beta u_s}{C_p} \quad (93)$$

For example, a 20 kbar shock wave alters intermolecular distance in tissue by approximately 10% and can heat the adjacent layers to  $\Delta T \approx 57^\circ \text{C}$ .

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